

1. Өнцөгийн хэмжээг радианаар илэрхийл.

1)  $15^{\circ} =$

2)  $30^{\circ} =$

3)  $40^{\circ} =$

4)  $50^{\circ} =$

5)  $60^{\circ} =$

6)  $800^{\circ} =$

7)  $90^{\circ} =$

8)  $100^{\circ} =$

9)  $135^{\circ} =$

10)  $150^{\circ} =$

11)  $270^{\circ} =$

12)  $360^{\circ} =$

2. Өнцөгийн хэмжээг градусаар илэрхийл.

1)  $\frac{\pi}{18} =$

2)  $\frac{\pi}{12} =$

3)  $\frac{\pi}{10} =$

4)  $\frac{\pi}{9} =$

5)  $\frac{\pi}{6} =$

6)  $\frac{\pi}{4} =$

7)  $\frac{\pi}{3} =$

8)  $\frac{\pi}{5} =$

9)  $\frac{2\pi}{5} =$

10)  $\frac{5\pi}{6} =$

11)  $\frac{3\pi}{2} =$

12)  $\frac{7\pi}{3} =$

13)  $\frac{3\pi}{4} =$

14)  $\frac{9\pi}{4} =$

3. Адилтгалыг батал.

1)  $\cos^2\alpha - 1 = -\sin^2\alpha$

2)  $1 - 2\sin^2\alpha = 2\cos^2\alpha - 1$

3)  $\sin^2\alpha \cdot \sin^2\beta + \sin^2\alpha \cdot \cos^2\beta + \cos^2\alpha = 1$

4)  $\cos^4\alpha - \sin^4\alpha = \cos^2\alpha - \sin^2\alpha$

5)  $(1 + \operatorname{tg}^2\alpha)(1 - \sin^2\alpha) - \sin^2\alpha = \cos^2\alpha$

6)  $\operatorname{tg}^2\alpha \cdot \operatorname{ctg}^2\alpha - \cos^2\alpha = \sin^2\alpha$

7)  $\sin^4\alpha + \cos^4\alpha = 1 - 2\sin^2\alpha \cdot \cos^2\alpha$

8)  $\sin^6\alpha + \cos^6\alpha + 3\sin^2\alpha \cdot \cos^2\alpha = 1$

9)  $2(\sin^6\alpha + \cos^6\alpha) - 3(\sin^4\alpha + \cos^4\alpha) + 1 = 0$

10)  $\frac{\operatorname{tg}x}{\sin x} - \frac{\sin x}{\operatorname{ctg}x} = \cos x$

11)  $\sin\left(\frac{\pi}{2} - x\right) = \cos x$

12)  $\cos\left(\frac{\pi}{2} - x\right) = \sin x$

13)  $\operatorname{tg}\left(\frac{\pi}{2} - x\right) = \operatorname{ctg}x$

14)  $\operatorname{ctg}\left(\frac{\pi}{2} - x\right) = \operatorname{tg}x$

15)  $\frac{\cos\alpha + \sin\alpha}{\cos\alpha - \sin\alpha} = \operatorname{tg}(45^{\circ} + \alpha)$

16)  $\frac{\cos\alpha + 1}{\sin\alpha} = \operatorname{ctg}\frac{\alpha}{2}$

17)  $\frac{\sin\alpha}{1 - \cos\alpha} = \operatorname{ctg}\frac{\alpha}{2}$

4. Тригонометр функцийн утгыг ол.

- 1)  $\sin\alpha = 0.6$  ба  $\frac{\pi}{2} < \alpha < \pi$  бол  $\cos\alpha, \operatorname{tg}\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 2)  $\operatorname{tg}\alpha = \sqrt{3}$  ба  $\pi < \alpha < \frac{3\pi}{2}$  бол  $\cos\alpha, \sin\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 3)  $\sin\alpha = -\frac{20}{29}$  ба  $\pi < \alpha < \frac{3\pi}{2}$  бол  $\cos\alpha, \operatorname{tg}\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 4)  $\operatorname{ctg}\alpha = -3$  ба  $\frac{3\pi}{2} < \alpha < 2\pi$  бол  $\cos\alpha, \operatorname{tg}\alpha, \sin\alpha$  – ийг ол.
- 5)  $\operatorname{tg}\alpha = 4\sqrt{3}$  ба  $0 < \alpha < \frac{\pi}{2}$  бол  $\cos\alpha, \sin\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 6)  $\operatorname{tg}\alpha = -\frac{40}{9}$  ба  $\frac{3\pi}{2} < \alpha < 2\pi$  бол  $\cos\alpha, \sin\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 7)  $\cos\alpha = -\frac{60}{61}$  ба  $\pi < \alpha < \frac{3\pi}{2}$  бол  $\sin\alpha, \operatorname{tg}\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 8)  $\operatorname{tg}\alpha = -1$  ба  $\frac{3\pi}{2} < \alpha < 2\pi$  бол  $\cos\alpha, \sin\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 9)  $\sin\alpha = -\frac{84}{85}$  ба  $\frac{3\pi}{2} < \alpha < 2\pi$  бол  $\cos\alpha, \operatorname{tg}\alpha, \operatorname{ctg}\alpha$  – ийг ол.
- 10)  $\operatorname{ctg}\alpha = -5$  ба  $\frac{\pi}{2} < \alpha < \pi$  бол  $\sin\alpha, \operatorname{tg}\alpha, \sin\alpha$  – ийг ол.

#### 5. Утгийг ол.

- 1)  $\sin 43^\circ \cdot \cos 17^\circ + \cos 43^\circ \cdot \sin 17^\circ =$
  - 2)  $\sin 56^\circ \cdot \cos 34^\circ + \cos 56^\circ \cdot \sin 34^\circ =$
  - 3)  $\cos 83^\circ \cdot \cos 7^\circ - \sin 83^\circ \cdot \sin 7^\circ =$
  - 4)  $\cos 37^\circ \cdot \cos 7^\circ + \sin 37^\circ \cdot \sin 7^\circ =$
  - 5)  $\frac{\operatorname{tg} 12^\circ + \operatorname{tg} 48^\circ}{1 - \operatorname{tg} 12^\circ \cdot \operatorname{tg} 48^\circ} =$
  - 6)  $\frac{\operatorname{ctg} 21^\circ \cdot \operatorname{ctg} 24^\circ - 1}{\operatorname{ctg} 21^\circ + \operatorname{ctg} 24^\circ} =$
  - 7)  $\frac{\sin 42^\circ \cdot \cos 18^\circ + \cos 42^\circ \cdot \sin 18^\circ}{\sin 14^\circ \cdot \cos 74^\circ - \cos 14^\circ \cdot \sin 74^\circ} =$
  - 8)  $\frac{\operatorname{ctg} 46^\circ \cdot \operatorname{ctg} 1^\circ + 1}{\operatorname{ctg} 46^\circ - \operatorname{ctg} 1^\circ} =$
- 9)  $\sin 15^\circ =$       12)  $\cos 15^\circ =$       15)  $\operatorname{tg} 75^\circ =$   
 10)  $\sin 75^\circ =$       13)  $\cos 75^\circ =$       16)  $\operatorname{ctg} 15^\circ =$   
 11)  $\sin 105^\circ =$       14)  $\operatorname{tg} 15^\circ =$       17)  $\operatorname{ctg} 75^\circ =$

#### 6. Тригонометр илэрхийлэлийг хялбарчил.

- 1)  $\sin^2\alpha + \sin^2\alpha \cdot \cos^2\alpha + \cos^4\alpha =$
- 2)  $\cos^2\alpha + \cos^2\alpha \cdot \sin^2\alpha + \sin^4\alpha - 1 =$
- 3)  $\frac{1}{\sin\alpha \cdot \cos\alpha} - \operatorname{ctg}\alpha =$
- 4)  $\frac{1}{\sin\alpha \cdot \cos\alpha} - \operatorname{tg}\alpha =$
- 5)  $(1 - \sin^2\alpha) \cdot (1 + \operatorname{tg}^2\alpha) =$
- 6)  $(1 - \cos^2\alpha) \cdot (1 + \operatorname{ctg}^2\alpha) =$
- 7)  $(\sin\alpha + \cos\alpha)^2 - 2\sin\alpha \cdot \cos\alpha =$
- 8)  $(\sin\alpha - \cos\alpha)^2 + 2\sin\alpha \cdot \cos\alpha =$
- 9)  $\sin^4\beta + \cos^4\beta + 2\sin^2\beta\cos^2\beta =$
- 10)  $1 - \frac{\sin\alpha \cdot \cos\alpha}{\operatorname{ctg}\alpha} =$
- 11)  $1 - \frac{\sin\alpha \cdot \cos\alpha}{\operatorname{tg}\alpha} =$
- 12)  $\frac{\operatorname{tg}\alpha \cdot \operatorname{ctg}\alpha - \cos^2\alpha}{2\sin\alpha} =$
- 13)  $1 - \frac{\sin^2\alpha}{1 - \cos\alpha} =$
- 14)  $1 - \frac{\sin^2\alpha}{1 + \cos\alpha} =$
- 15)  $\frac{1 - \operatorname{tg}^2\alpha}{1 + \operatorname{tg}^2\alpha} =$
- 16)  $\operatorname{tg}^2\beta \cdot (2\cos^2\beta + \sin^2\beta - 1) =$
- 17)  $\operatorname{ctg}^2\beta \cdot (2\sin^2\beta + \cos^2\beta - 1) =$
- 18)  $\frac{\sin^3\alpha + \cos^3\alpha}{\sin\alpha + \cos\alpha} + \sin\alpha \cdot \cos\alpha =$
- 19)  $\frac{\sin^3\alpha - \cos^3\alpha}{\sin\alpha - \cos\alpha} - \sin\alpha \cdot \cos\alpha =$

- 20)  $\frac{\sin^3\alpha + \cos^3\alpha}{\sin\alpha + \cos\alpha} + \sin\alpha \cdot \cos\alpha =$
- 21)  $\frac{\sin^3\alpha - \cos^3\alpha}{\sin\alpha - \cos\alpha} - \sin\alpha \cdot \cos\alpha =$
- 22)  $\frac{1}{\cos\alpha} - \frac{\cos\alpha}{1 + \sin\alpha} =$
- 23)  $\frac{1}{\sin\alpha} - \frac{\sin\alpha}{1 + \cos\alpha} =$
- 24)  $3\sin^4\alpha - 2\sin^6\alpha + 3\cos^4\alpha - 2\cos^6\alpha =$
- 25)  $\cos^2\alpha + \operatorname{tg}^2\alpha \cdot \cos^2\alpha =$
- 26)  $\sin^2\alpha + \operatorname{ctg}^2\alpha \cdot \sin^2\alpha =$
- 27)  $\frac{\sin^2x - 1}{\cos^2x - 1} =$
- 28)  $\cos^2x \cdot (1 + \operatorname{tg}^2x) - \sin^2x =$
- 29)  $\frac{\sin\alpha}{1 - \cos\alpha} + \frac{\sin\alpha}{1 + \cos\alpha} =$
- 30)  $\frac{1}{1 + \sin\alpha} + \frac{1}{1 - \sin\alpha} =$
- 31)  $\frac{1 + \operatorname{tg}x + \operatorname{tg}^2\alpha}{1 + \operatorname{ctg}\alpha + \operatorname{ctg}^2\alpha} =$
- 32)  $\frac{1}{1 + \operatorname{tg}^2\alpha} + \frac{1}{1 + \operatorname{ctg}^2\alpha} =$
- 33)  $\frac{\sin^2\alpha - \cos^2\alpha + \cos^4\alpha}{\cos^2\alpha - \sin^2\alpha + \sin^4\alpha} =$
- 34)  $(\cos\alpha - \sin\alpha)^2 + (\cos\alpha + \sin\alpha)^2 =$
- 35)  $\operatorname{ctg}\alpha + \frac{\sin\alpha}{1 + \cos\alpha} =$
- 36)  $\operatorname{tg}\alpha + \frac{\cos\alpha}{1 + \sin\alpha} =$

Хариу:

4. Тригонометр функцийн утгыг ол.

1.  $\cos\alpha = -\frac{4}{5}$ ,  $\operatorname{tg}\alpha = -\frac{3}{4}$ ,  $\operatorname{ctg}\alpha = -\frac{4}{3}$     2.  $\cos\alpha = -\frac{1}{2}$ ,  $\sin\alpha = -\frac{\sqrt{3}}{2}$ ,  $\operatorname{ctg}\alpha = \frac{1}{\sqrt{3}}$   
3.  $\cos\alpha = -\frac{21}{29}$ ,  $\operatorname{tg}\alpha = \frac{20}{21}$ ,  $\operatorname{ctg}\alpha = \frac{21}{20}$     4.  $\cos\alpha = \frac{3}{\sqrt{10}}$ ,  $\operatorname{tg}\alpha = -\frac{1}{3}$ ,  $\sin\alpha = -\frac{1}{\sqrt{10}}$   
5.  $\cos\alpha = \frac{12}{7\sqrt{3}}$ ,  $\sin\alpha = \frac{1}{7}$ ,  $\operatorname{tg}\alpha = \frac{\sqrt{3}}{12}$     6.  $\cos\alpha = \frac{9}{41}$ ,  $\operatorname{ctg}\alpha = -\frac{9}{40}$ ,  $\sin\alpha = -\frac{40}{41}$   
7.  $\sin\alpha = -\frac{11}{61}$ ,  $\operatorname{ctg}\alpha = \frac{60}{11}$ ,  $\operatorname{tg}\alpha = \frac{11}{60}$     8.  $\cos\alpha = \frac{\sqrt{2}}{2}$ ,  $\operatorname{ctg}\alpha = -1$ ,  $\sin\alpha = -\frac{\sqrt{2}}{2}$   
9.  $\cos\alpha = \frac{13}{85}$ ,  $\operatorname{ctg}\alpha = -\frac{13}{84}$ ,  $\operatorname{tg}\alpha = -\frac{84}{13}$     10.  $\cos\alpha = -\frac{5\sqrt{26}}{26}$ ,  $\operatorname{tg}\alpha = -5$ ,  $\sin\alpha = \frac{\sqrt{26}}{26}$

5. Утгийг ол.

1.  $\frac{\sqrt{2}}{2}$     2. 1    3. 0    4.  $\frac{\sqrt{3}}{2}$     5.  $\sqrt{3}$     6. 1    7. -1    8. 1  
9.  $\frac{\sqrt{6}-\sqrt{2}}{4}$     10.  $\frac{\sqrt{6}+\sqrt{2}}{4}$     11.  $\frac{\sqrt{6}+\sqrt{2}}{4}$     12.  $\frac{\sqrt{6}+\sqrt{2}}{4}$     13.  $\frac{\sqrt{6}-\sqrt{2}}{4}$     14.  $2-\sqrt{3}$   
15.  $2+\sqrt{3}$     16.  $2+\sqrt{3}$     17.  $2-\sqrt{3}$

6. Тригонометр илэрхийлэлийг хялбарчил.

1. 1    2. 0    3.  $\operatorname{tg}\alpha$     4.  $\operatorname{ctg}\alpha$     5. 1    6. 1  
7. 1    8. 1    9. 1    10.  $\cos^2\alpha$     11.  $\sin^2\alpha$     12.  $\frac{\sin\alpha}{2}$   
13.  $-\cos\alpha$     14.  $\cos\alpha$     15.  $\cos 2\alpha$     16.  $\sin^2\alpha$     17.  $\cos^2\alpha$   
18.  $1-\frac{1}{2}\sin 2\alpha$     19.  $1+\frac{1}{2}\sin 2\alpha$     20. 1    21. 1    22.  $\operatorname{tg}\alpha$   
23.  $\operatorname{ctg}\alpha$     24. 1    25. 1    26. 1    27.  $\operatorname{ctg}^2\alpha$     28.  $1+\sin^2\alpha$   
29.  $\frac{2}{\sin^2\alpha}$     30.  $\frac{2}{\cos^2\alpha}$     31.  $\operatorname{tg}^2\alpha$     32. 1    33.  $\operatorname{tg}^4\alpha$     34. 2  
35.  $\frac{1}{\sin\alpha}$     36.  $\frac{1}{\cos\alpha}$